



*BioChips*



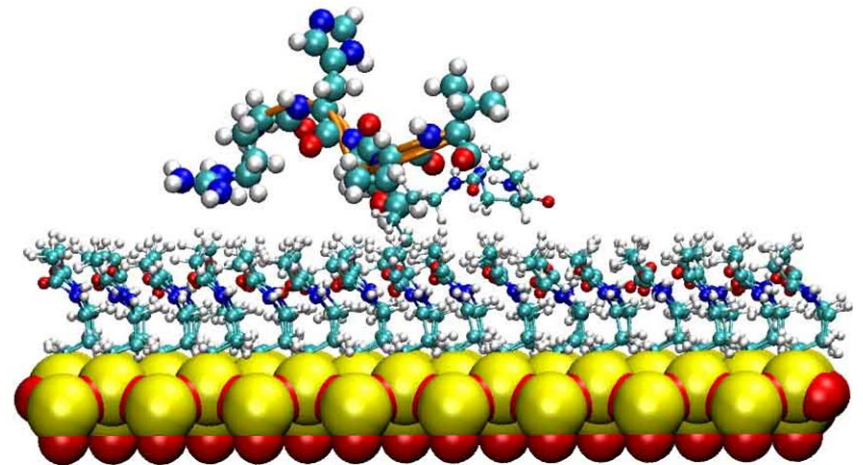
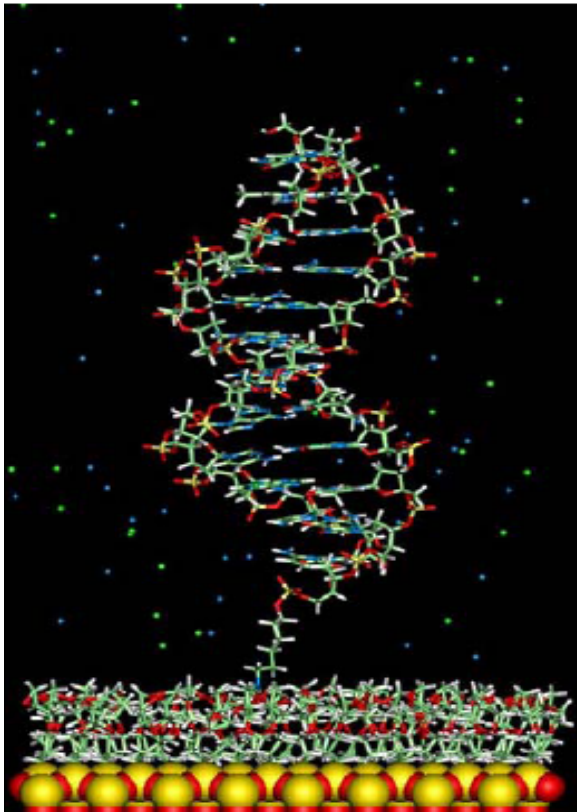
*Theory  
and  
Simulations*

# *Combination of hard and soft condensed matter*

- Hard surface for localization and/or electronics
- Soft biomolecule for tunable molecular recognition

# *Two examples*

## DNA Chips and Peptide Chips



# *DNA Chips*

*are useful for a variety of tasks*

- Disease detection
- Genetic analysis
- Computing

What are the design specific criteria for each usage?  
Sequence? Detection limits?

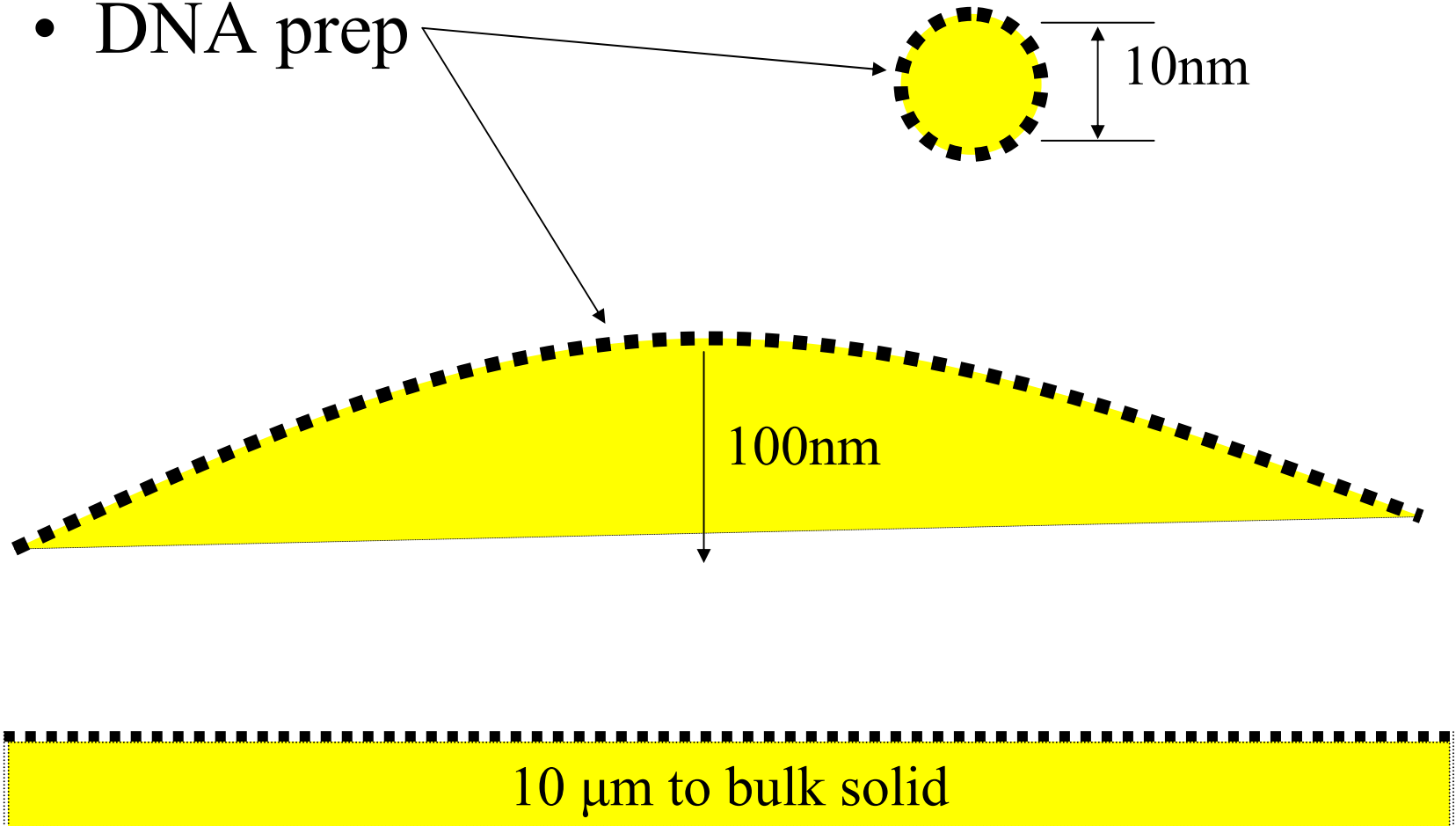
# *DNA Chips are an Industry*

- Currently  $O(\$1+\text{G}/\text{yr})$
- Potential to be  $O(\$100\text{G}/\text{yr})$

*QA/QC problems are  
Surface Science problems*

# *Materials and Size Matter*

- DNA prep



# ***The Experiment***

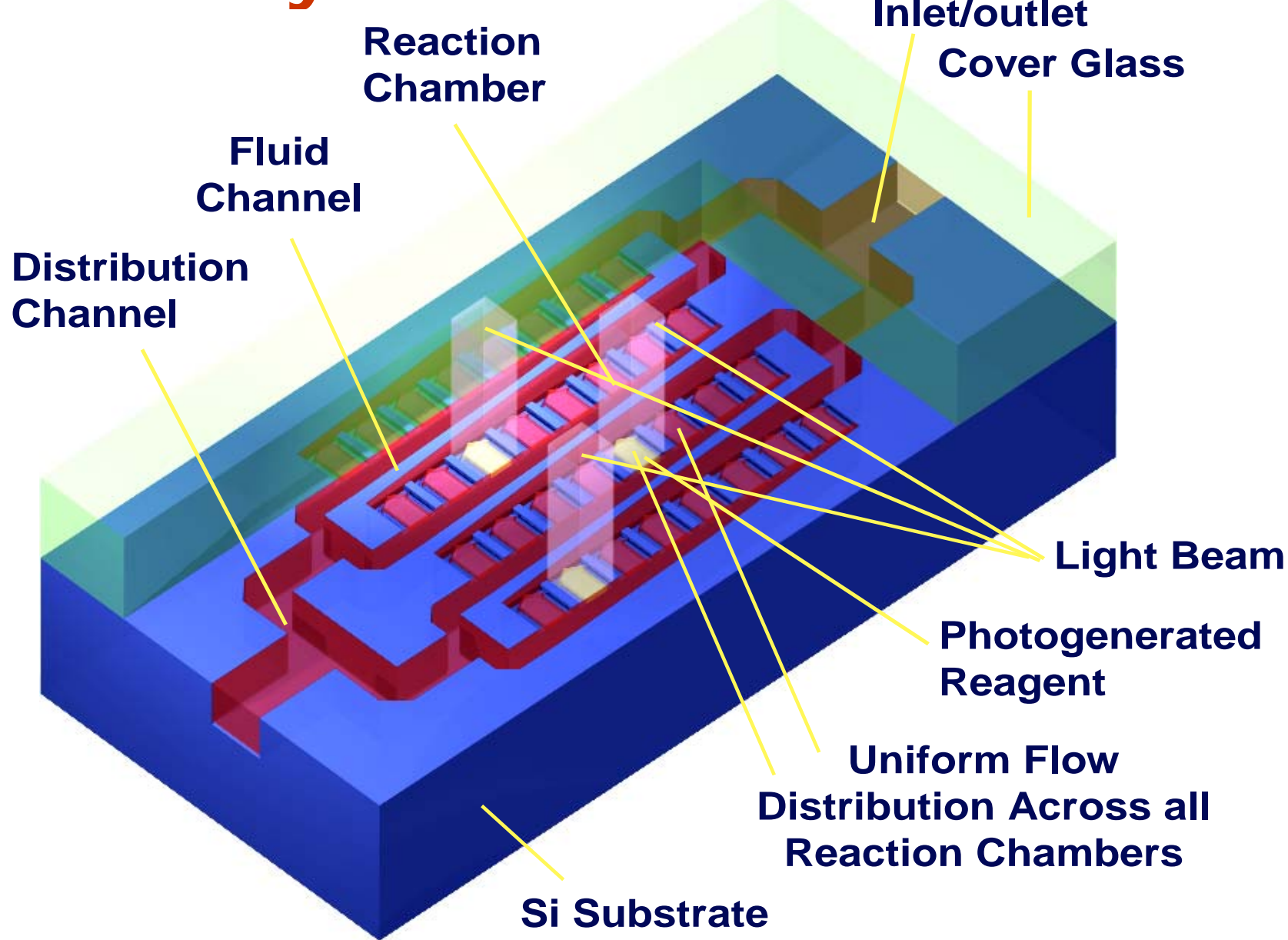
- ***Pick the sequences***
  - *genetic disease*
  - *cancer*
  - *retroviral genes*
  - *random to detect species*
- ***Smart synthesis with lithography***
- ***Control of purity during each step***
- ***Results & Analysis are not “yes or no”***

- *10,000 to 100,000 experiments or “reads”*

## *How to detect the signal?*

- *Use CCD's*
  - *Color sensitive*
  - *Intensity  $\propto$  Concentration*

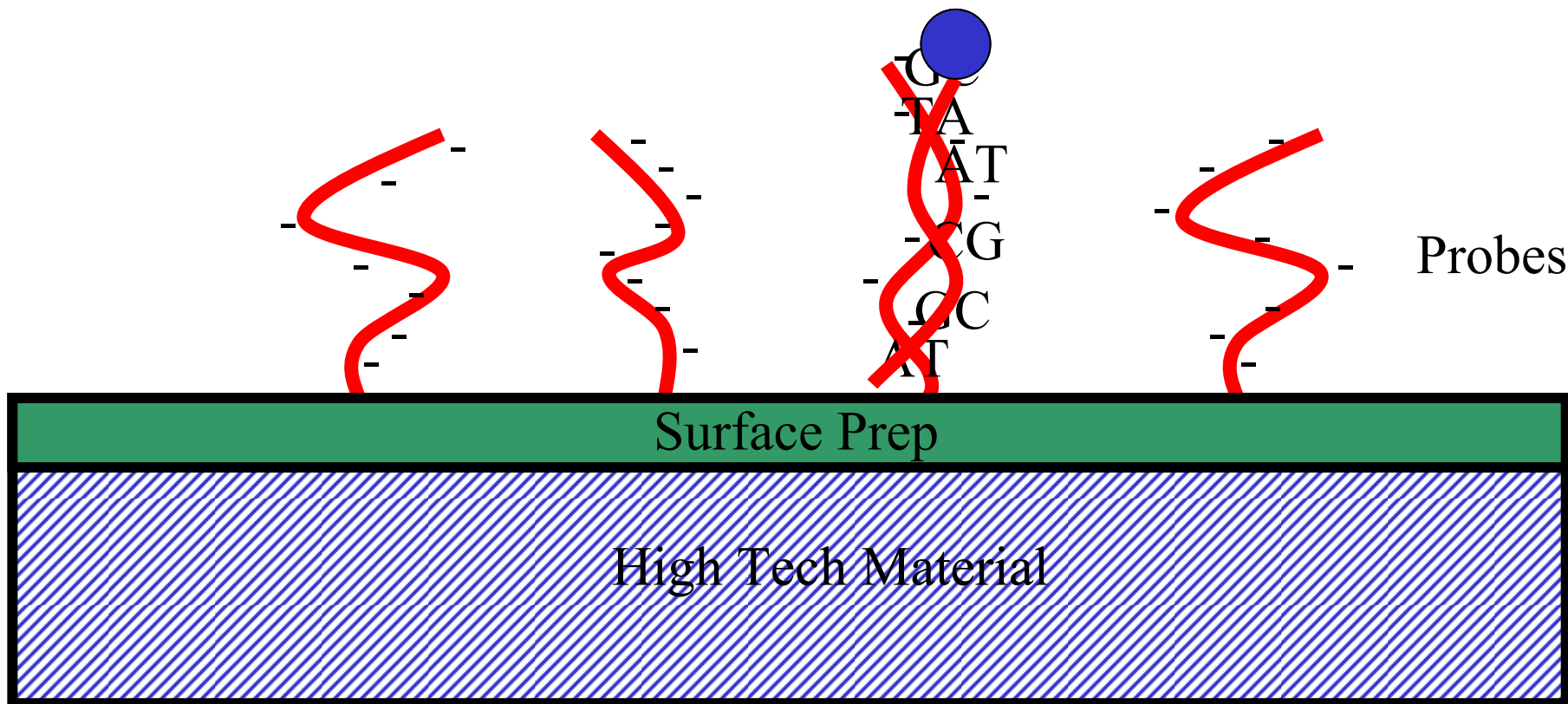




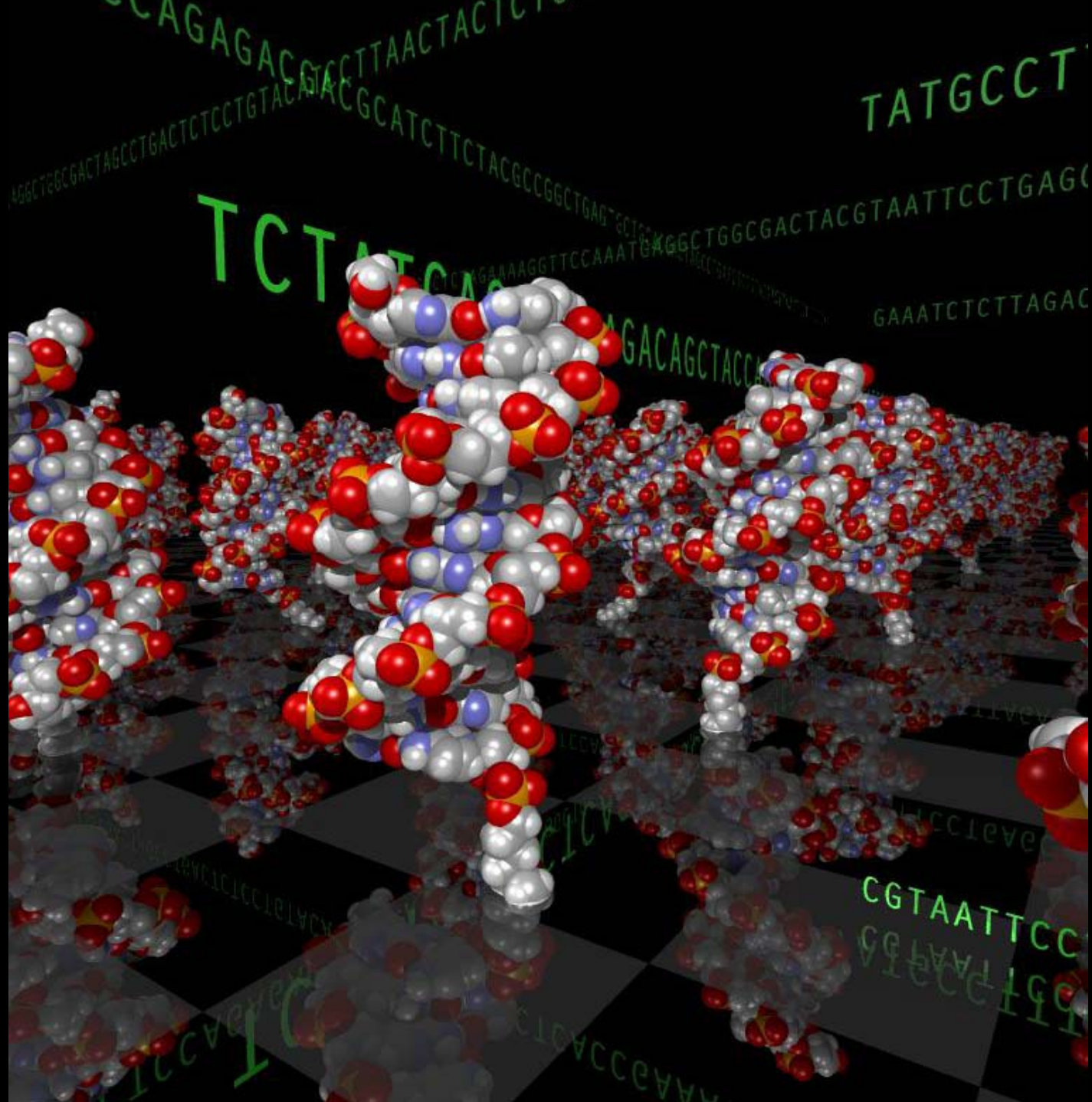


# *Salt Water*

Targets







# *Parallel Analysis*

The *equilibrium* during Hybridization Analysis results in *binary* mistakes in detection.

## Qualitative vs. Quantitative analysis

- **Presence** or **Absence** complicated by multiple misleading equilibria
- Poor sensitivity (broad melting curves)

# ***Problems in Microarrays***

## ***Effect Apparent Binding***

- Optimal surface preparation; shifts melting T
  - Dielectric, Metal, Hydrophobic moments ...
- Signal Strengths
  - 8+ orders of magnitude of intensity
- Spot size/shape distribution
  - Large deviations
  - Missing spots
- Purity of Probes on Surface
  - Chemistry
- Sample preparation
  - Biological prep, synchronization, pcr

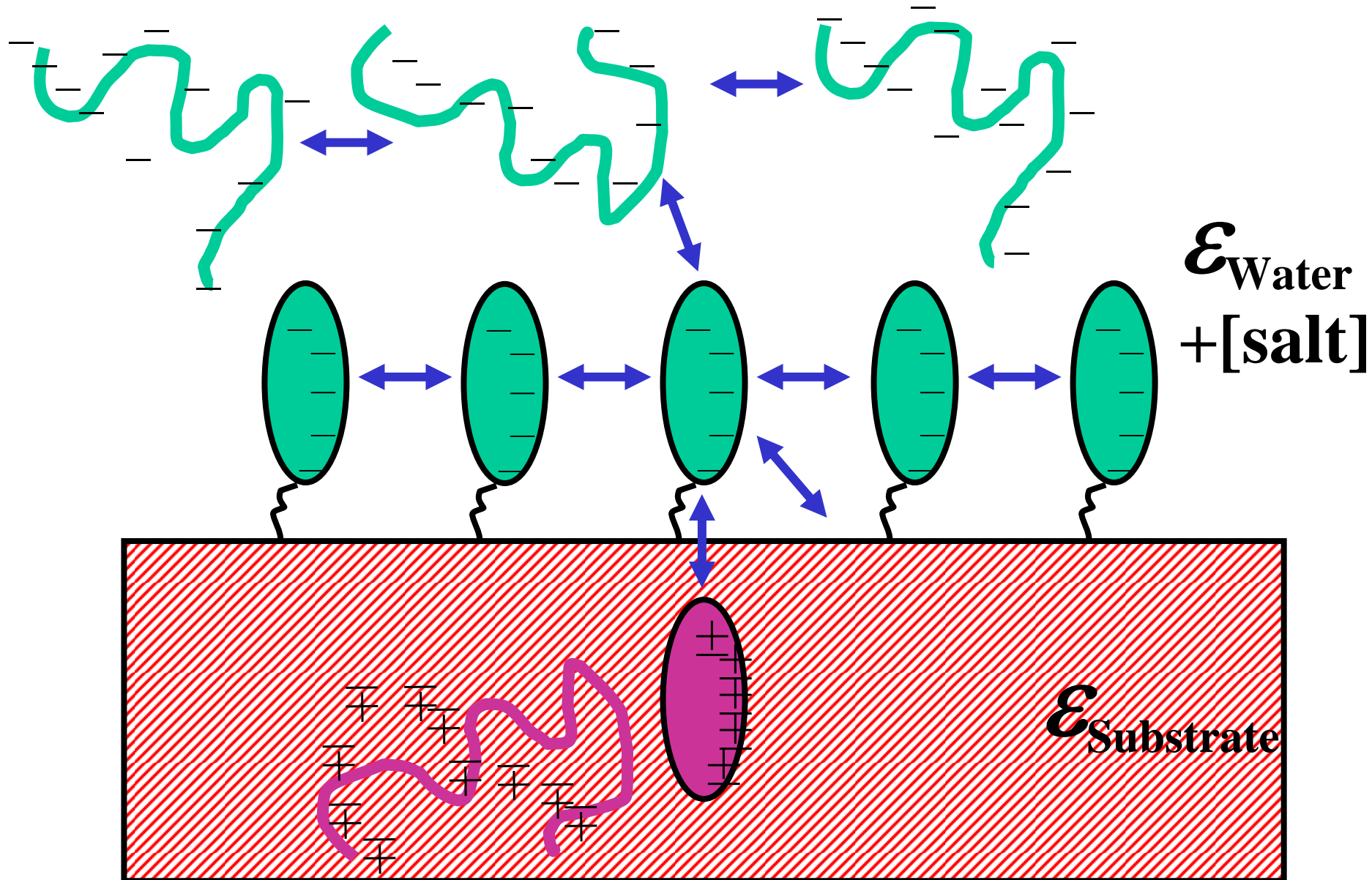
# *Basic Problem*

DNA binding is different in the presence of a surface than in homogeneous solution.

What are the causes?

How do we use the changes?

# *Forces: Surface and Solution*





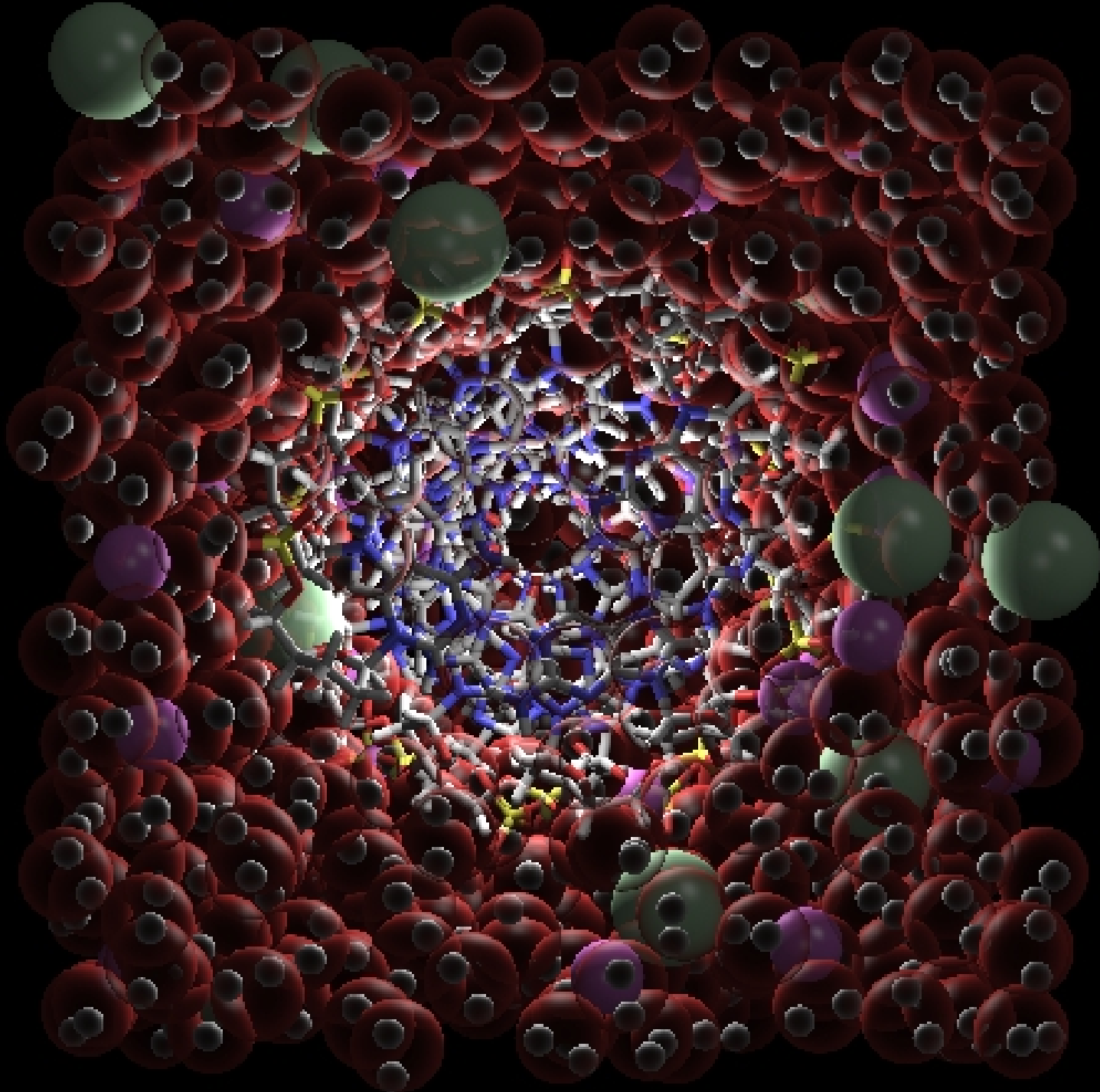
# *Two Design Areas*

- Target and Surface Probe interact with **Liquid-Solid Interface** (*repulsive or attractive*)

*Decreases with distance from Surface (linker length)*

- Multiple targets are Repelled by Probe array

*Increases with Probe surface concentration*

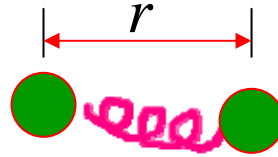


# Computer Simulations start with a force law:

## Classical in this case

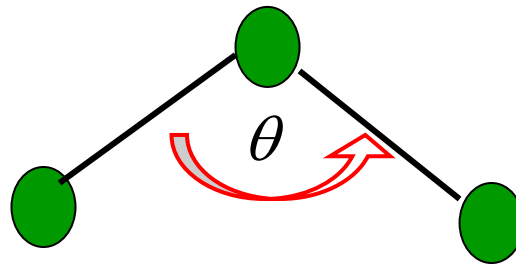
Bonds - 2 body term

- harmonic, Hook's Law spring



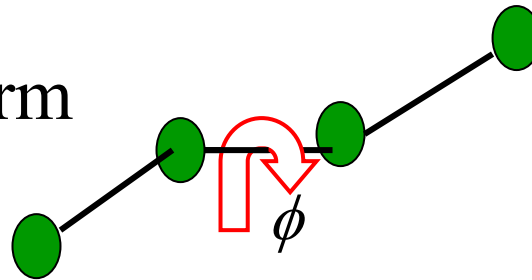
$$\sum_{bonds} K_b (r - r_e)^2$$

Angles - 3 body term



$$\sum_{angles} K_\theta (\theta - \theta_e)^2$$

Dihedrals - 4 body term



$$\sum_{torsions} K_\phi (1 + \cos(n\phi + \delta))$$

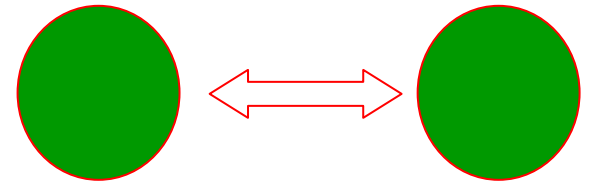
$n = \text{multiplicity}$

$\delta = \text{phase}$

Parameters come from experiments & quantum mechanical studies of small molecules that are chemically similar to segments of the molecule of interest.

## Nonbonded Terms

2 body terms



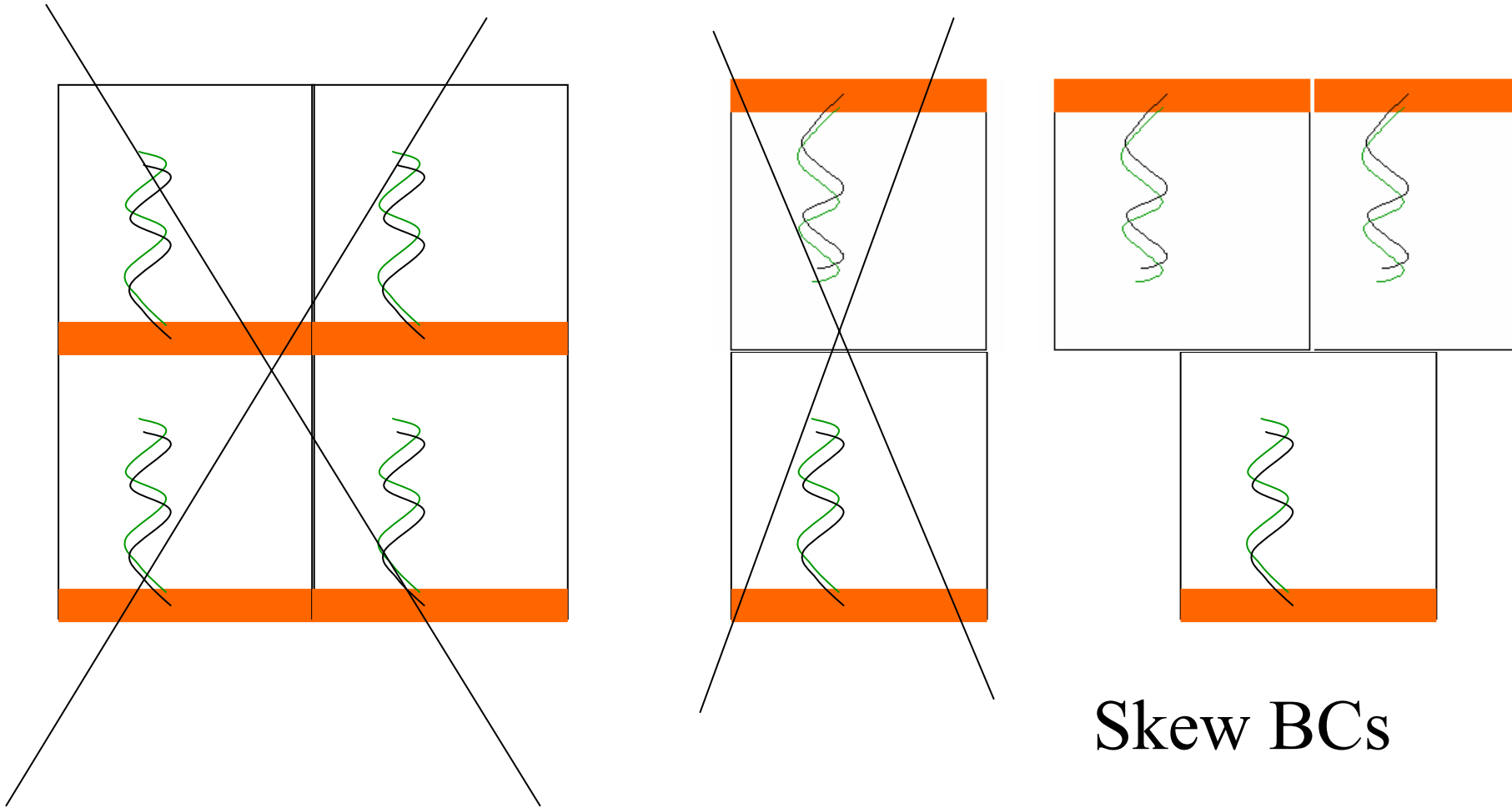
Coulombic & van der Waals

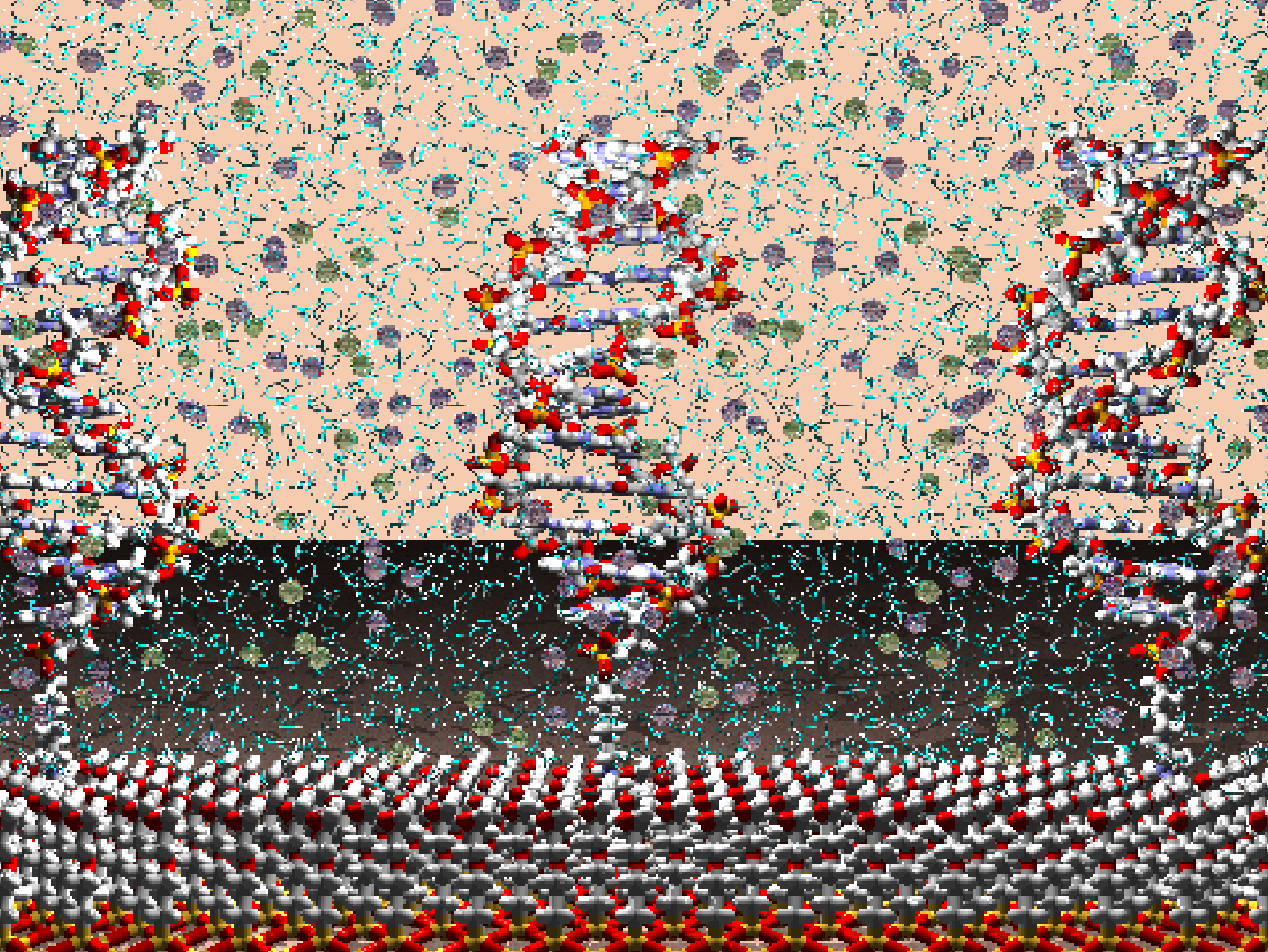
$$\sum_{\substack{\text{Nonbonded} \\ \text{pairs of atoms}}} 4\epsilon_{ij} \left( \left( \frac{\sigma_{ij}}{r} \right)^{12} - \left( \frac{\sigma_{ij}}{r} \right)^6 \right) + \frac{q_i q_j}{r}$$

Three body and higher nonbonded terms can be incorporated at great expense!

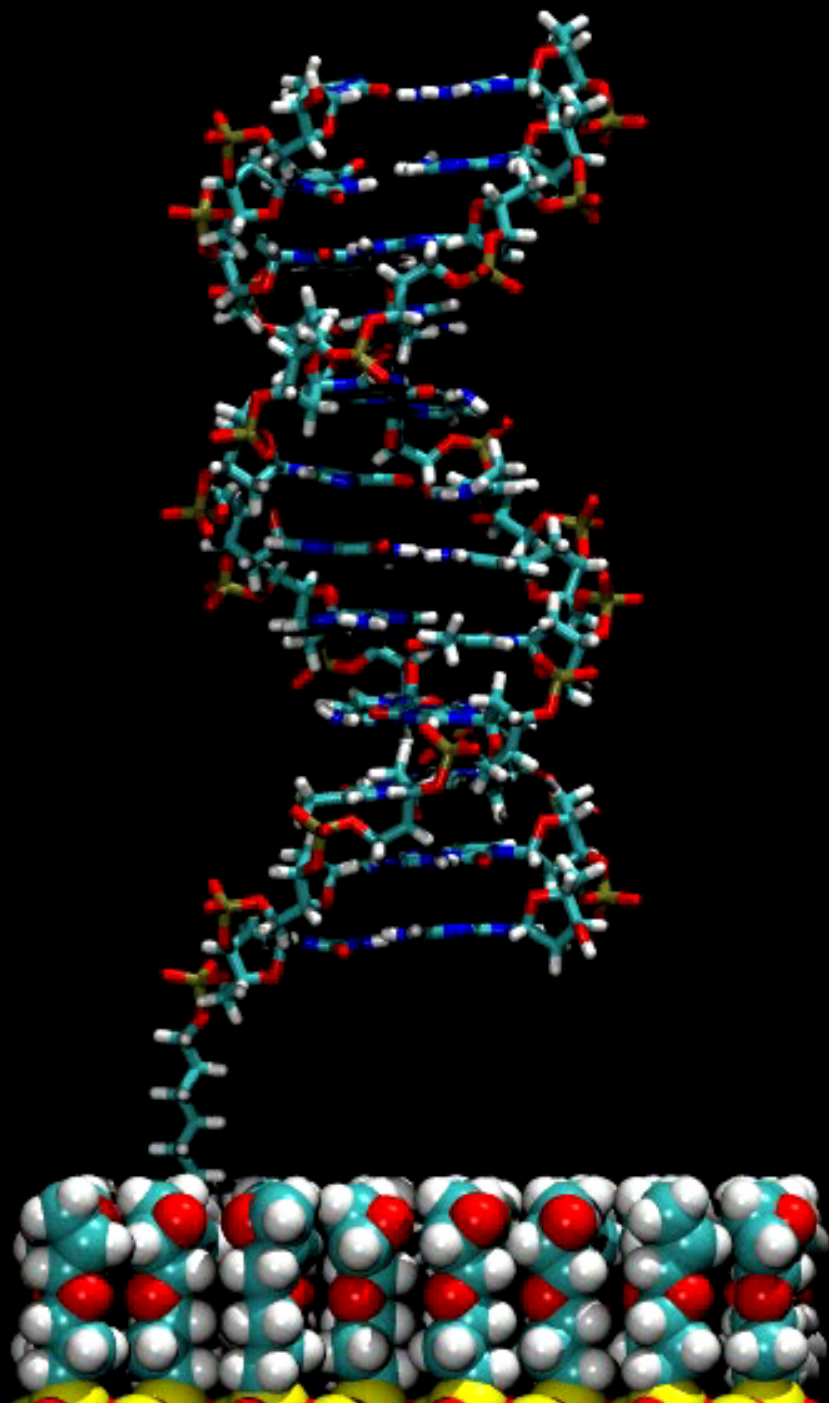
# Periodic Boundaries for Surfaces

## Lamellar mess; Change symmetry

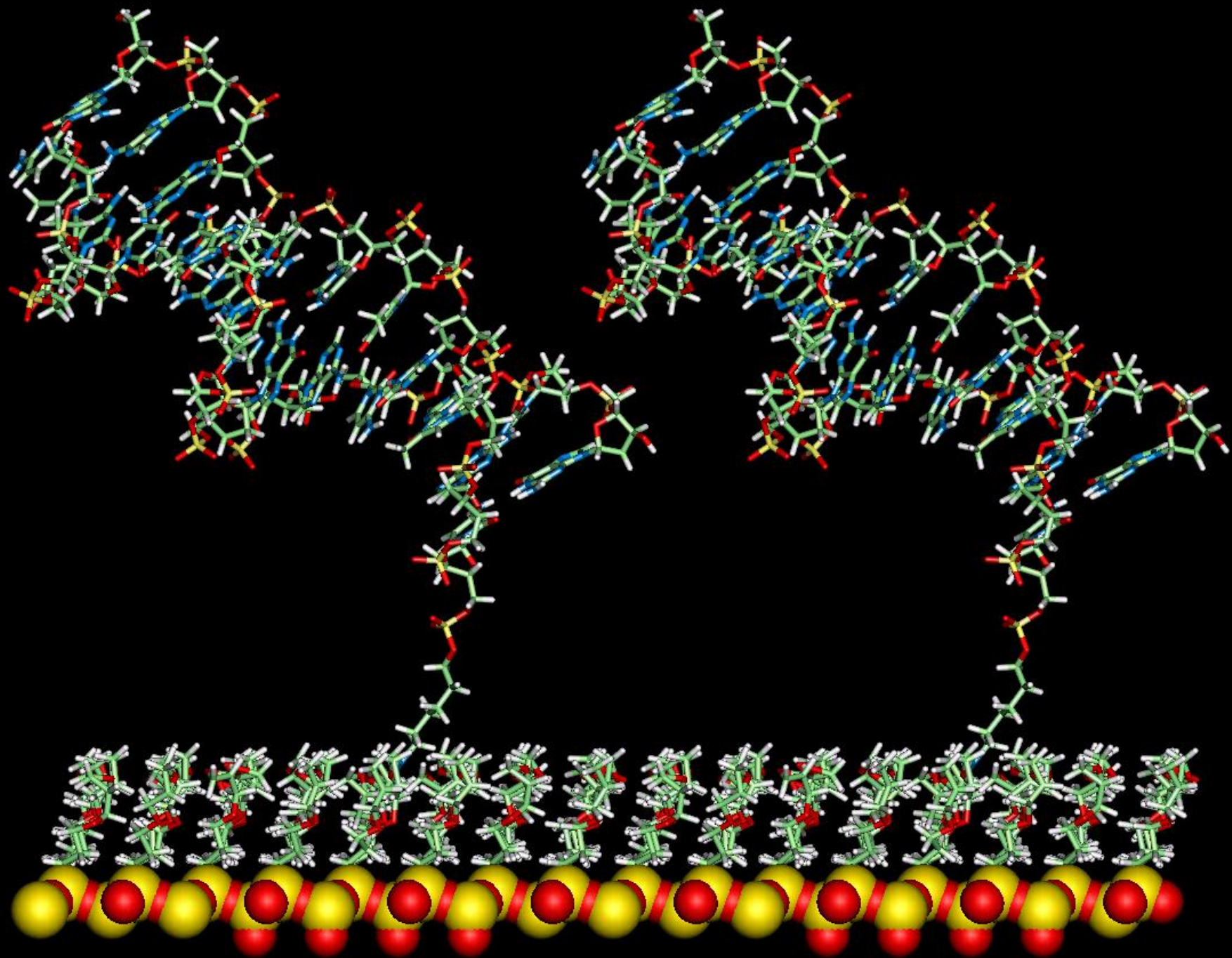




0 ns









# *Correlations*

- Neither Vertical nor Flat on surface (tilt)
- Low fraying (**tight** binding)
- Nonuniform Structures
- Linker/spacer effects

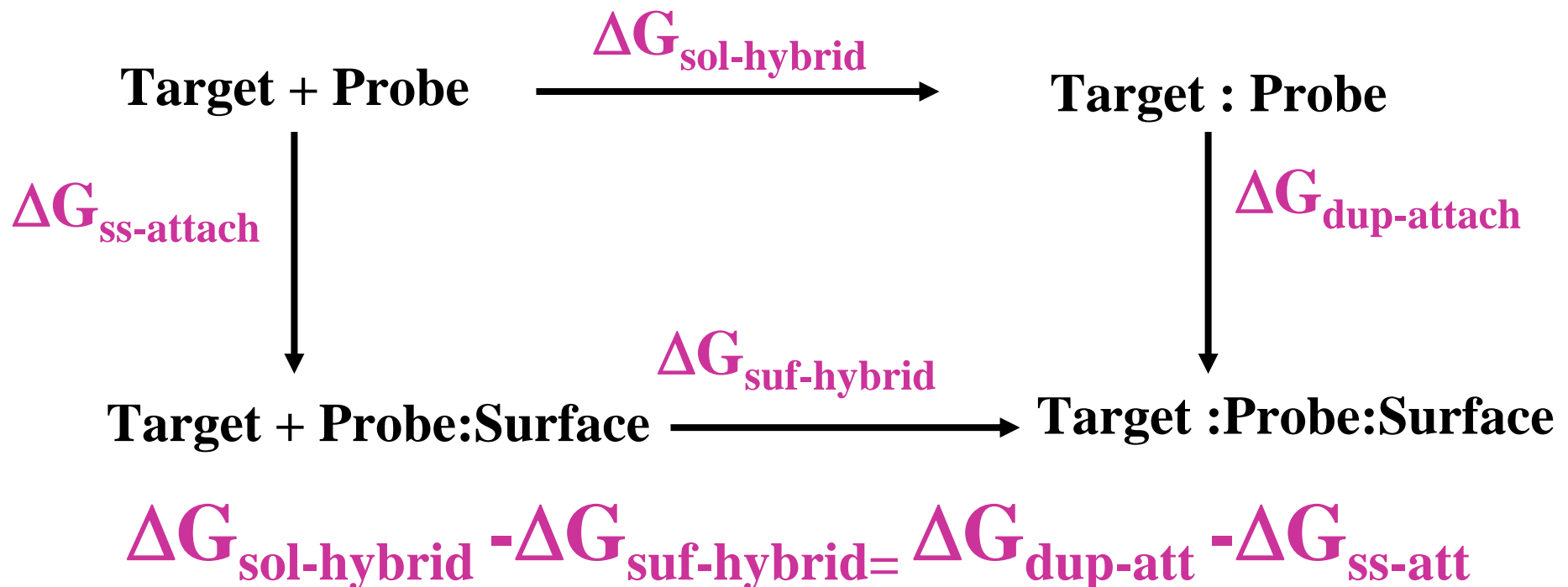
# *Implications*

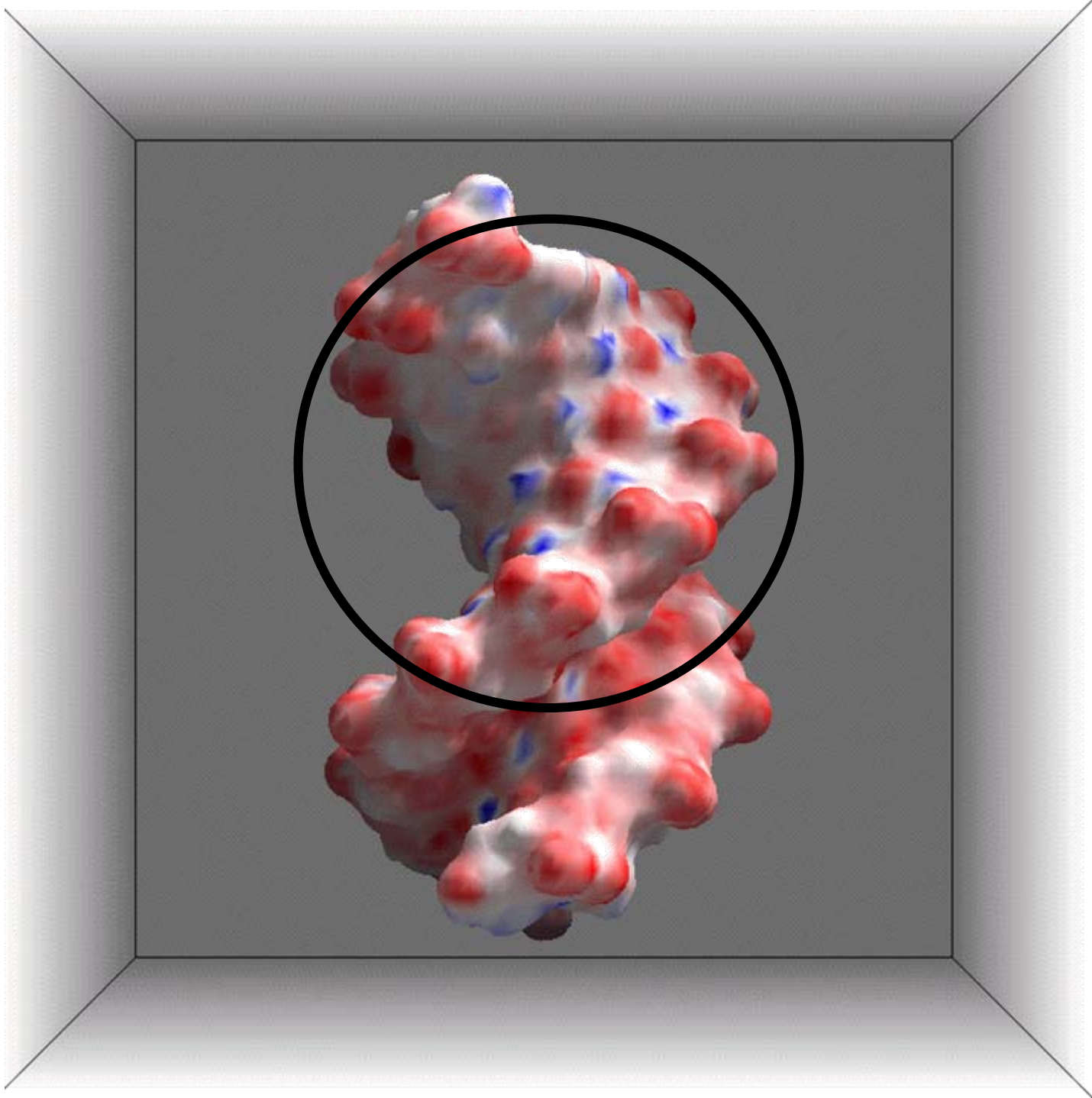
- Colloidal behavior affects
  - synthesis / fabrication
  - and binding
- Tilt restricts possible geometries of pairing
- Low fraying consistent with high affinity and good specificity at low target concentration

**$\Delta G$  &  $\Delta\Delta G$**

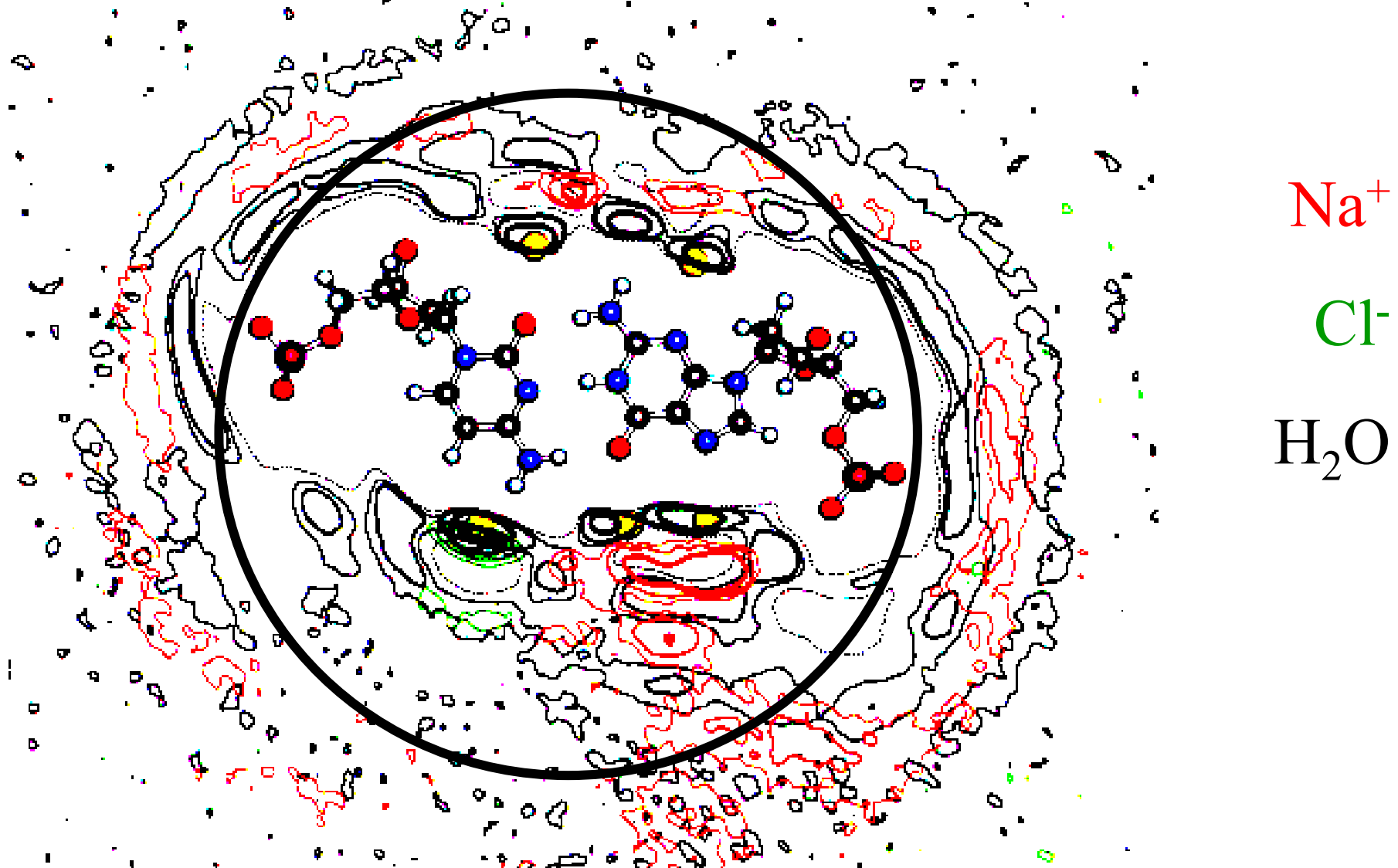
# Theory

*Object: to Analyze the free energy difference of hybridization between that in solution and on a surface*



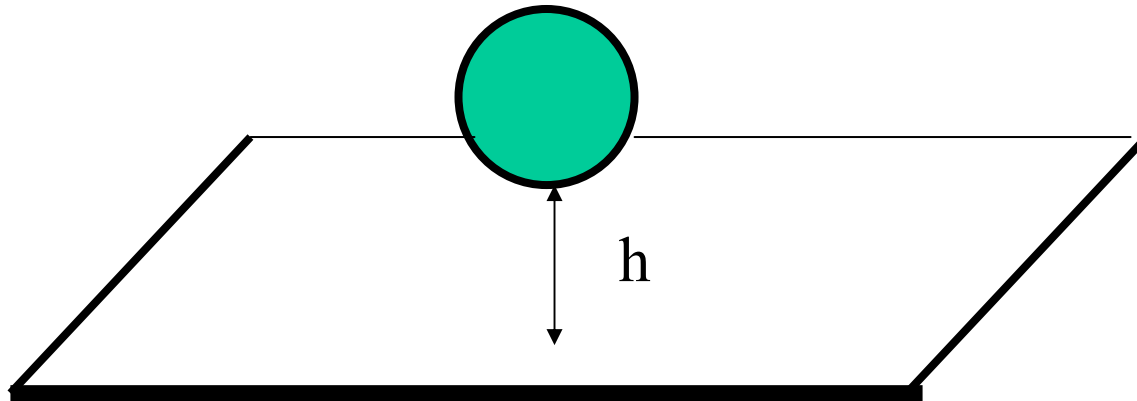


*The ions and water penetrate the grooves.*



# *Need a Simple Model*

- Ion permeable 20 Å spheroid over a plane/surface
  - 8 bp in aqueous saline solution over a surface
- Linear Poisson-Boltzmann has an  
analytic solution

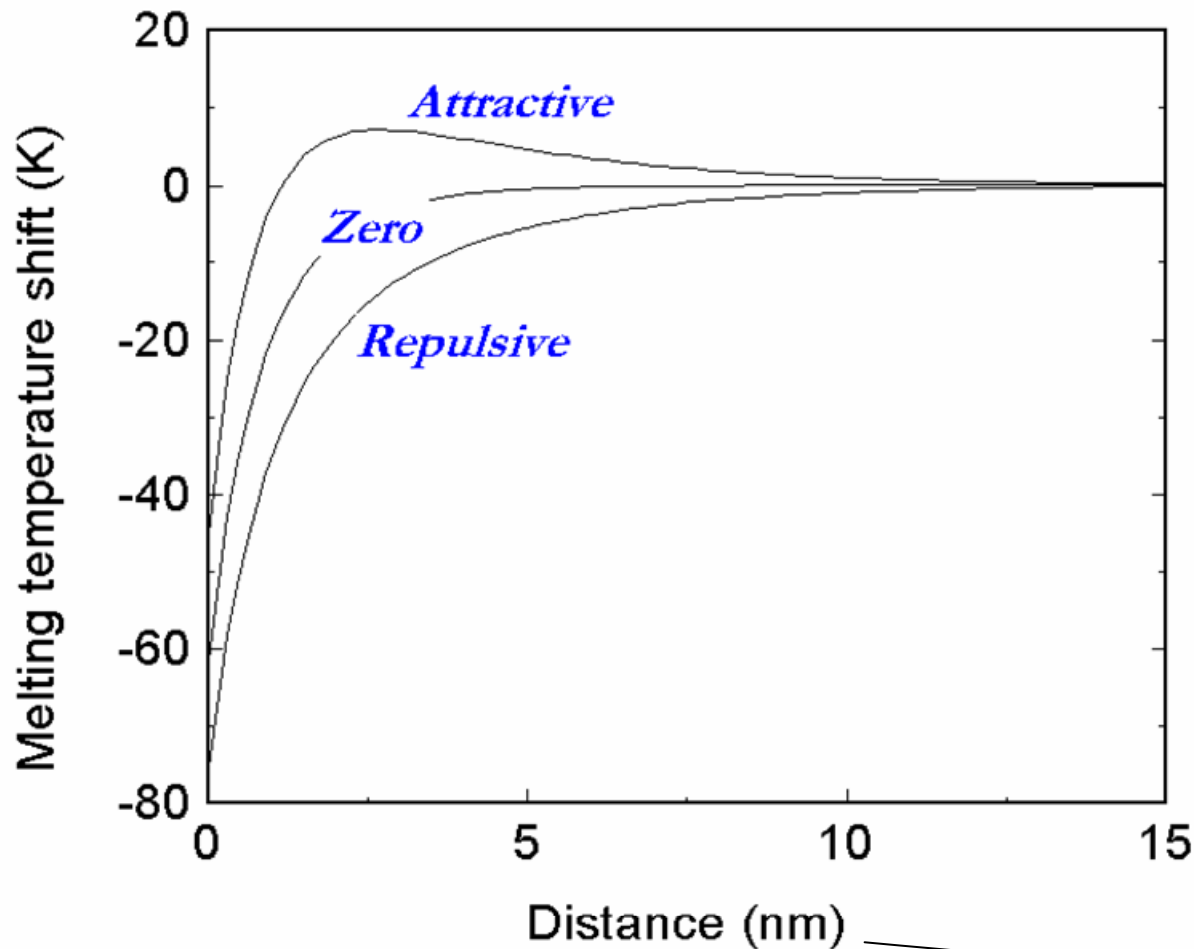


I.D. - Ohshima and Kondo, '93

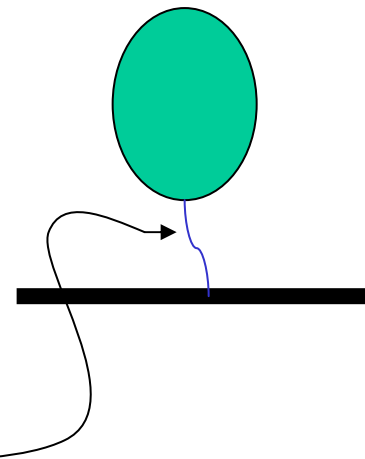
Finite C - Vainrub and Pettitt, '02

Elipsoidal Geometry- Garrido and Pettitt, '08

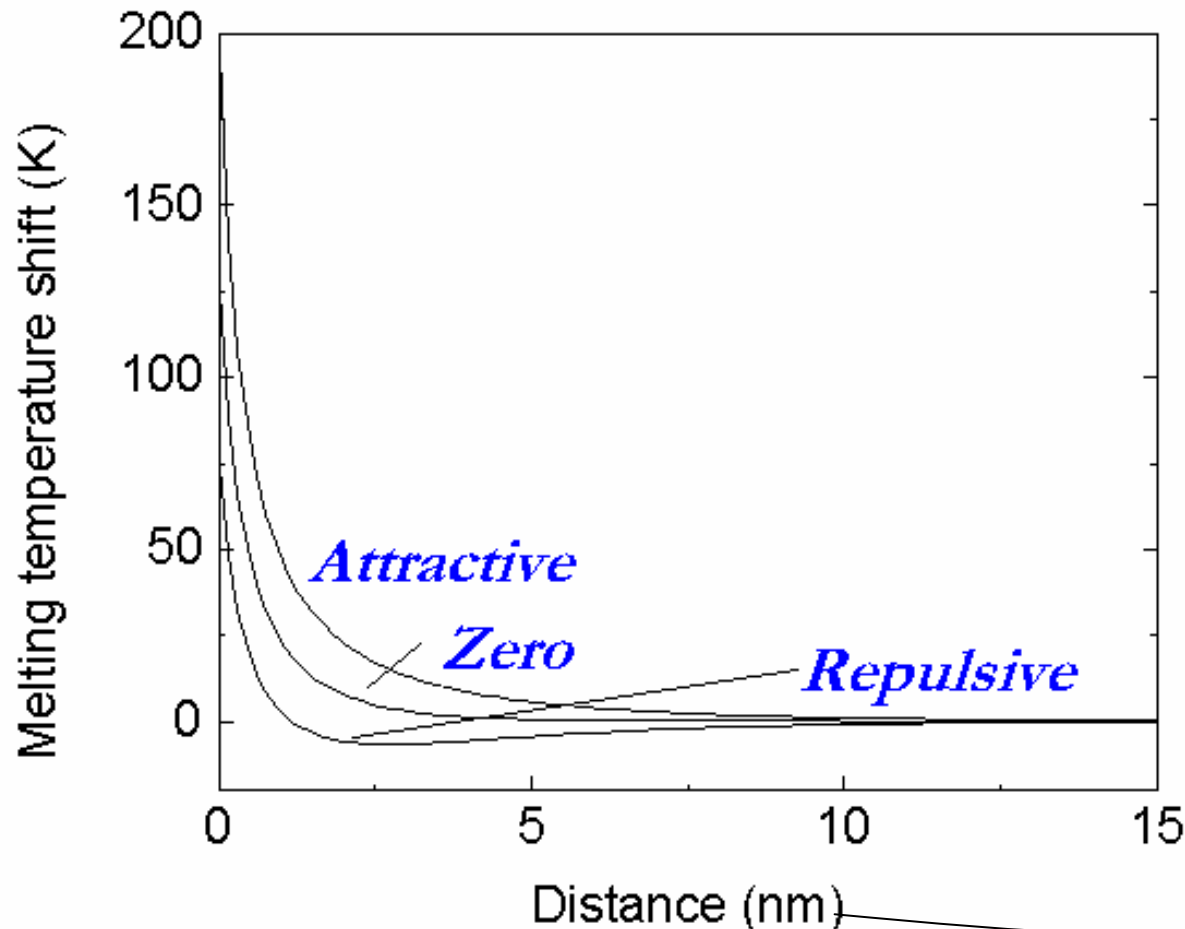
*The shift of the melting temperature for an immobilized 8 base pair oligonucleotide duplex at 0.01M NaCl as a function of the distance from a dielectric surface*



$q=0$  or  $\pm$   
 $0.36e/nm^2$



# *Surface at a constant potential for a metal coated substrate @ .01 M NaCl*



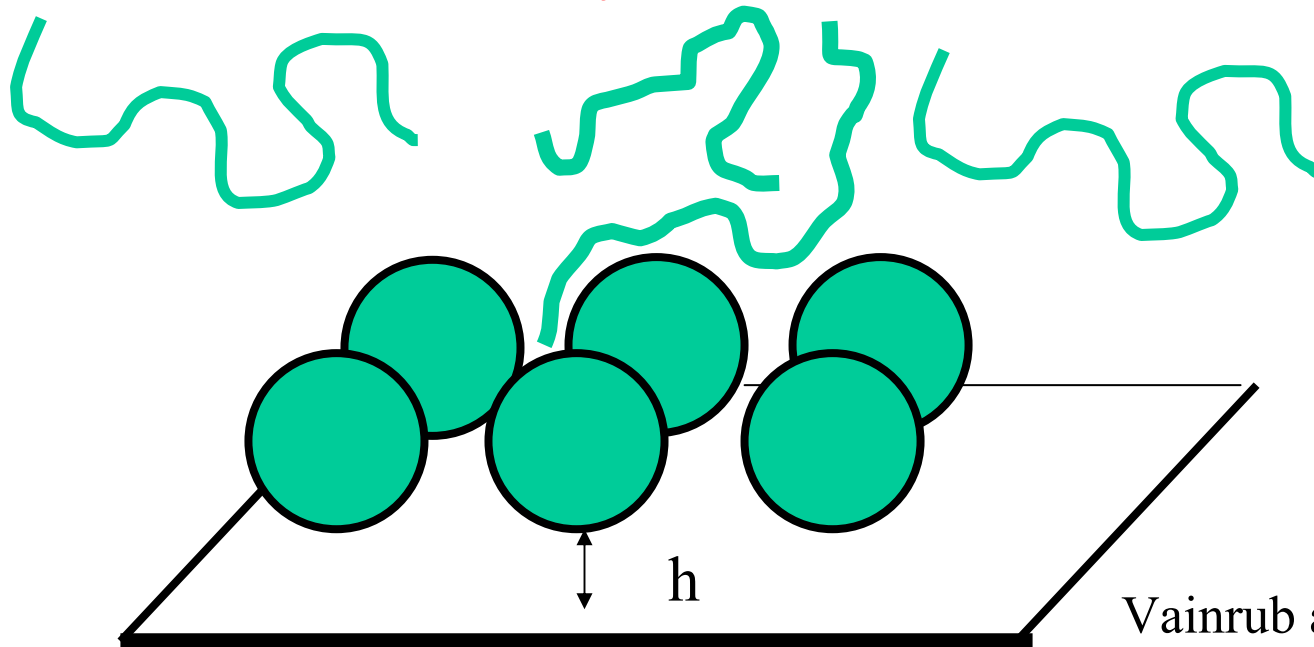


# *Effects of Crowding with High Coverage*

- Target Concentration
- Surface Coverage
- Tether Length
- Solvent Dielectric
- Salt Concentration

# *Yet Another Simple Model*

- Ion permeable 20 Å **spheres** over a plane/surface
  - in aqueous saline solution at finite density
- Linear Poisson-Boltzmann still has an  
**analytic solution**



# *Melting curve temperature and width vs. surface probe density (coverage) is simple*

**In solution**

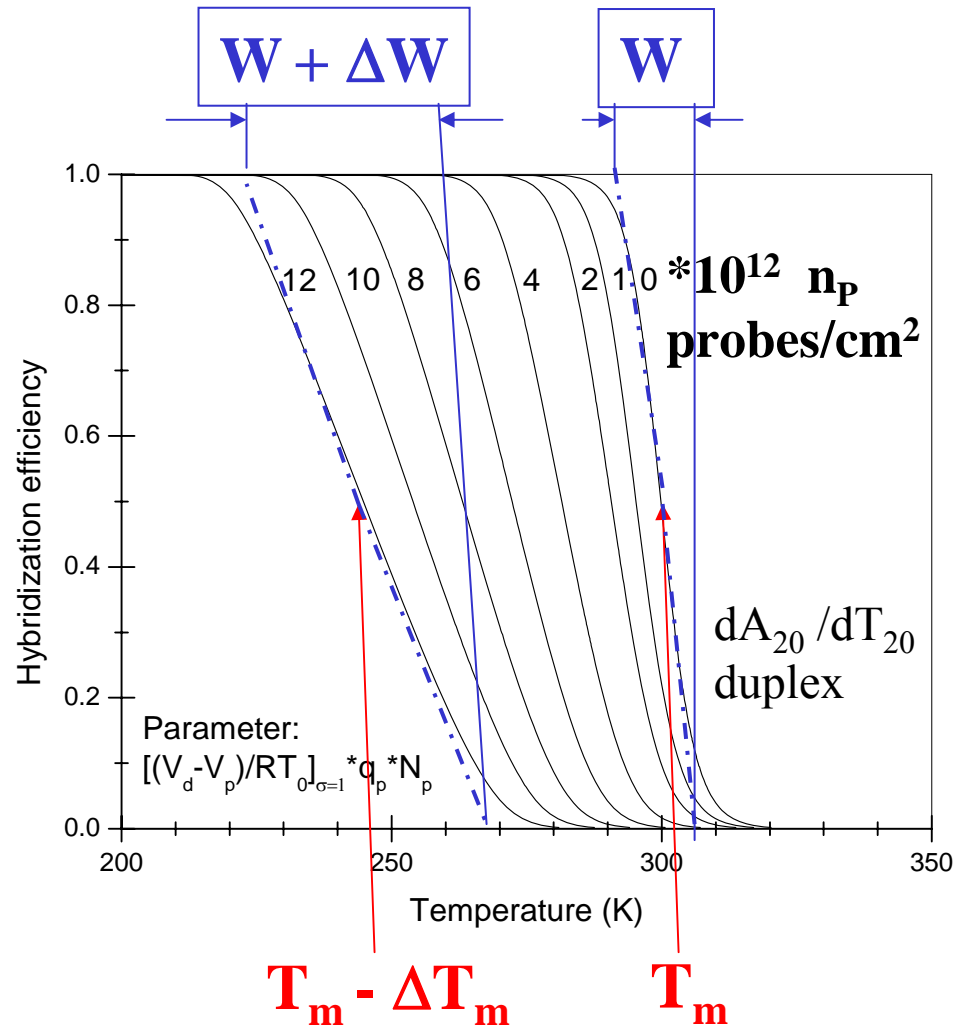
$$T_m = \Delta H_0 / (\Delta S_0 - R \ln C)$$

$$W = 4RT_m^2 / \Delta H_0$$

**On-array: Isotherms**

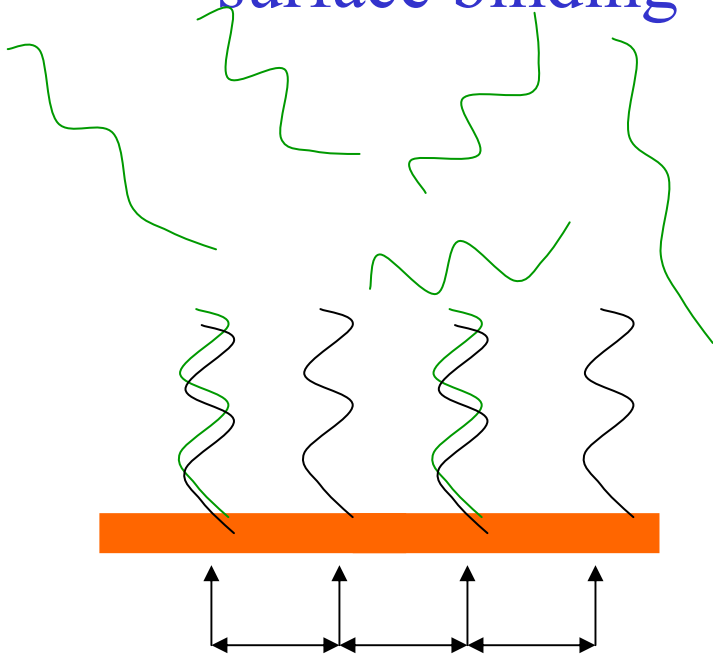
$$\Delta T_m = \frac{3wZ^2n_p}{2\Delta H_0 + 3wZ^2n_p}$$

$$\Delta W = \frac{2}{3} \Delta T_m$$

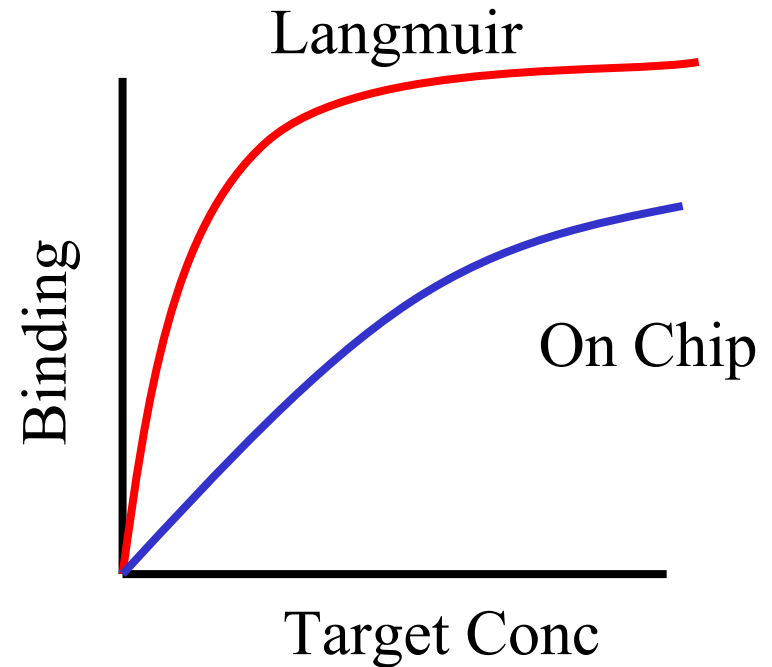


# ***Coulomb Blockage Dominates Optimum spacing***

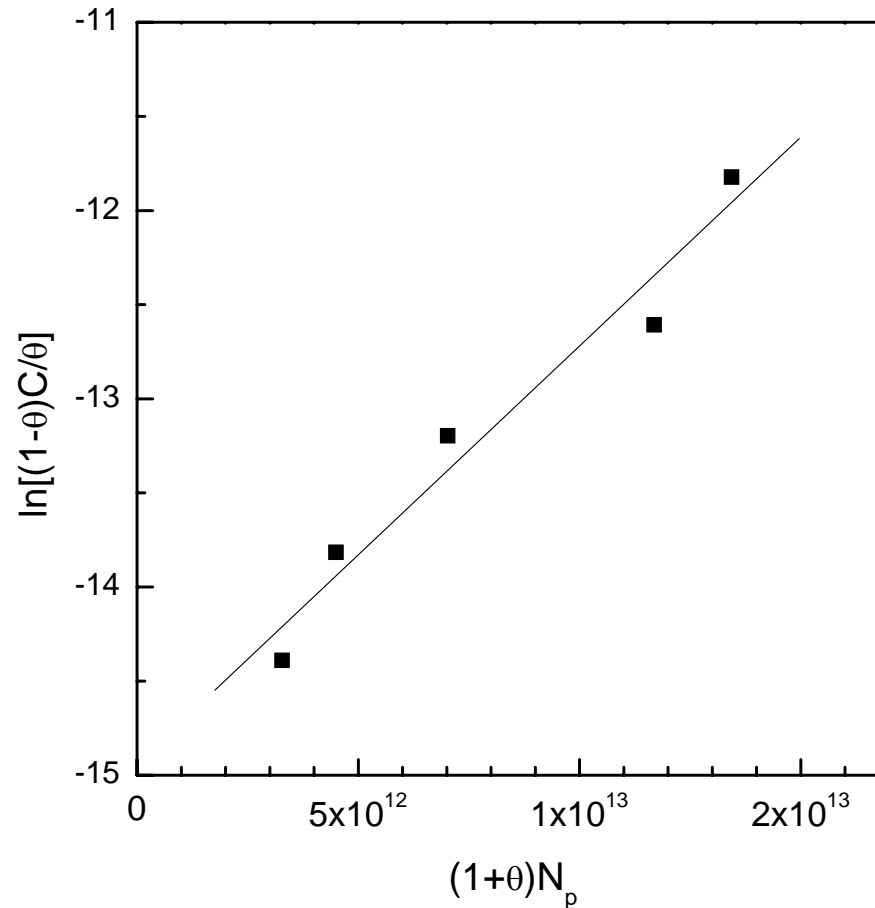
High negative charge  
density repels target  
surface binding



Probe surface density



# *Comparison with Experimental Isotherm*



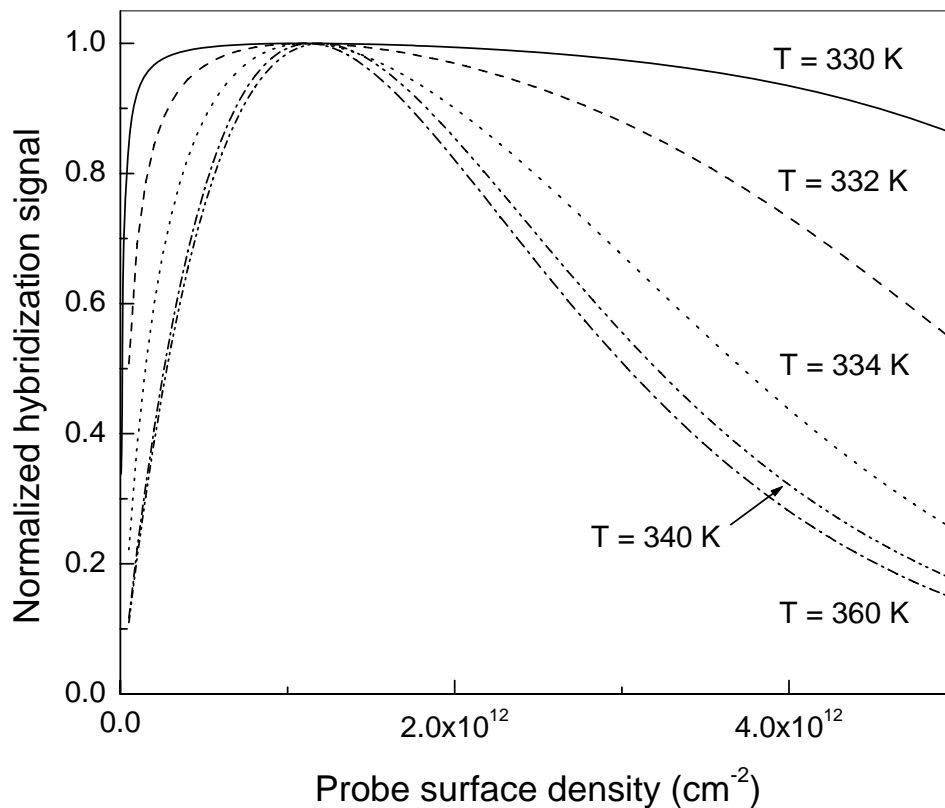
## **Accord with experiments:**

- Low on-array hybridization efficiency (Guo et al 1994, Shchepinov et al 1995)
- Broadening and down-temperature shift of melting curve (Forman et al 1998, Lu et al 2002)
- Surface probe density effects (Peterson et al 2001, Steel et al 1998, Watterson 2000)

# *Mean field predicts the Peak of sensitivity*

$$n_p = \frac{RT}{wZ_p^2}$$

Vainrub and Pettitt,  
JACS (2003)



# *cDNA arrays have more problems.*

What is the structure of DNA on a positively charged Surface?

(Poly-lysine or polyamines)

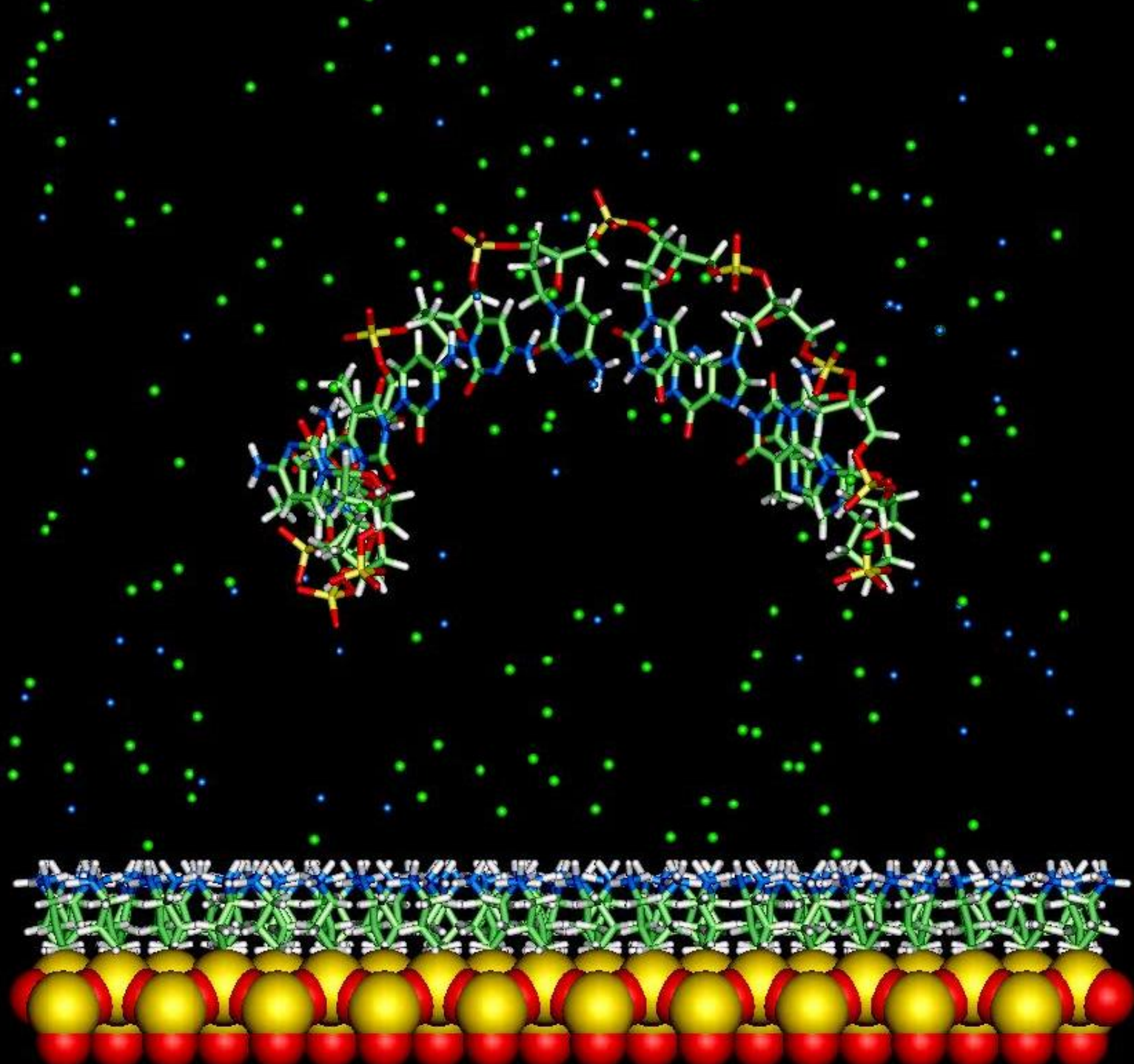
Surface experiments for structure are tough.

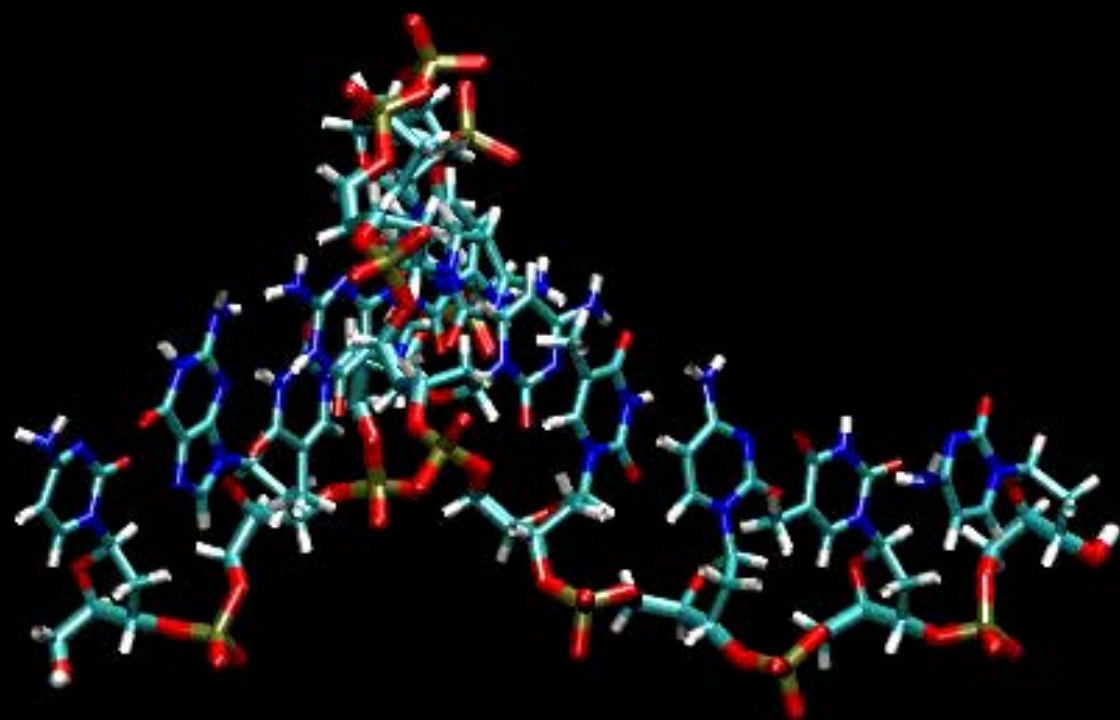
So simulate.

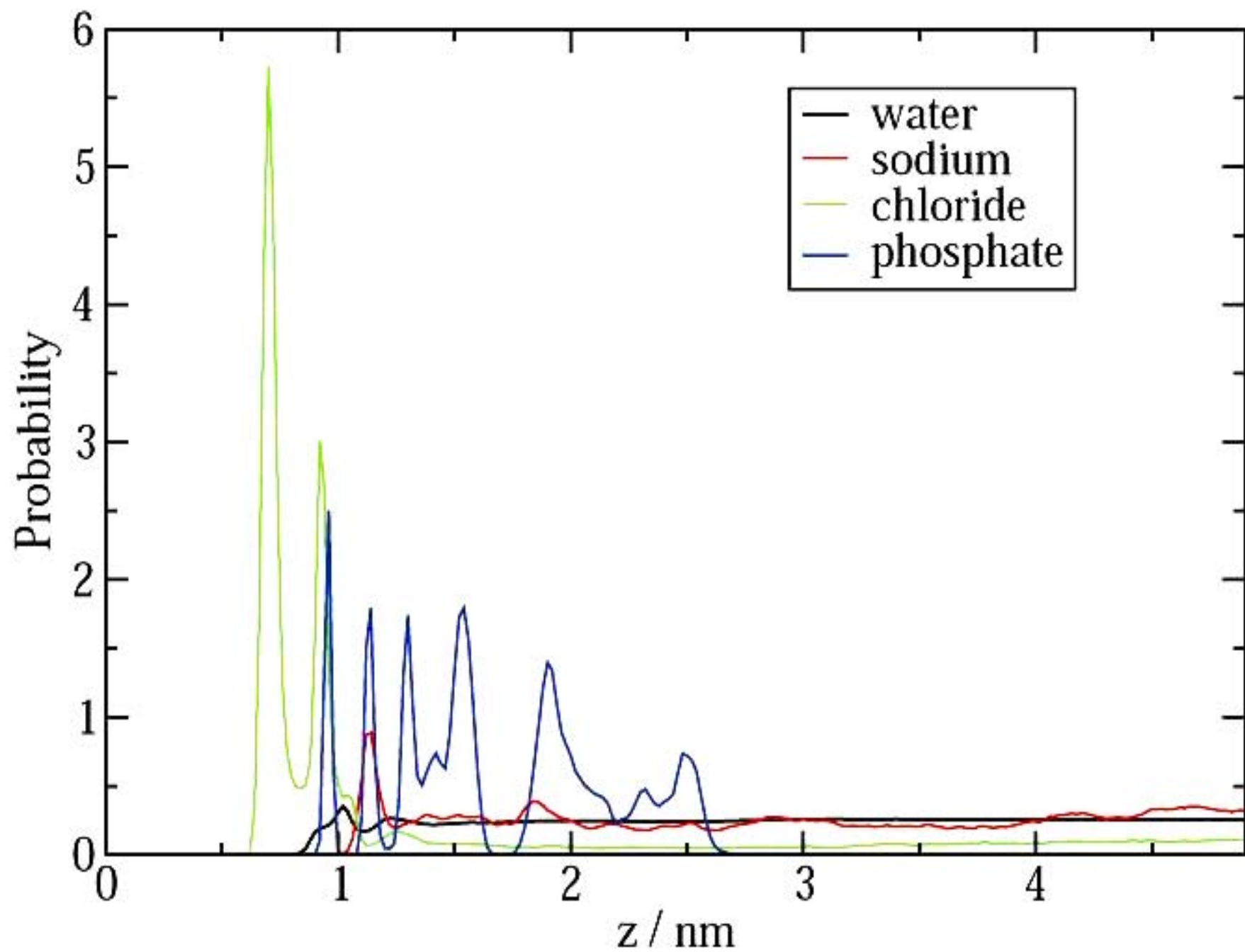
## *Near a charged surface*

- Different local ion conc.
- Reports of enhanced binding
- Reports of enhanced kinetics
- Same geometry?









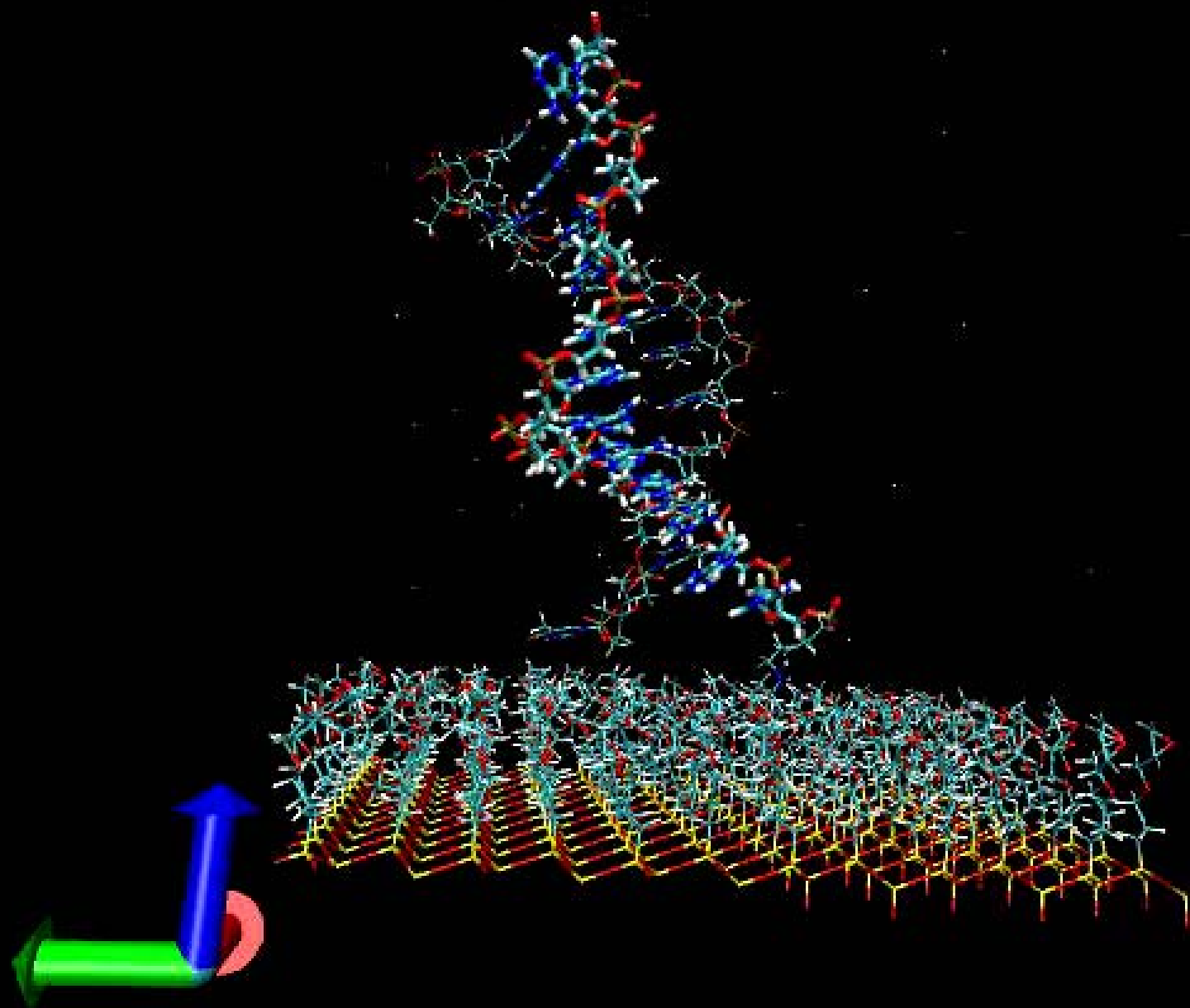
# *Lessons for Designs*

Sequence length determines criteria

- Potential Sequence-Information Content
- Melting Temperature Range
- Melting Temperature Width (SNPs)

Surface design affects detectability

Surface fidelity has large effects





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